

Limit Load Analysis of suction anchors for cohesive materials

By Dr Amir Rahim

The CRISP Consortium Ltd/South Bank University

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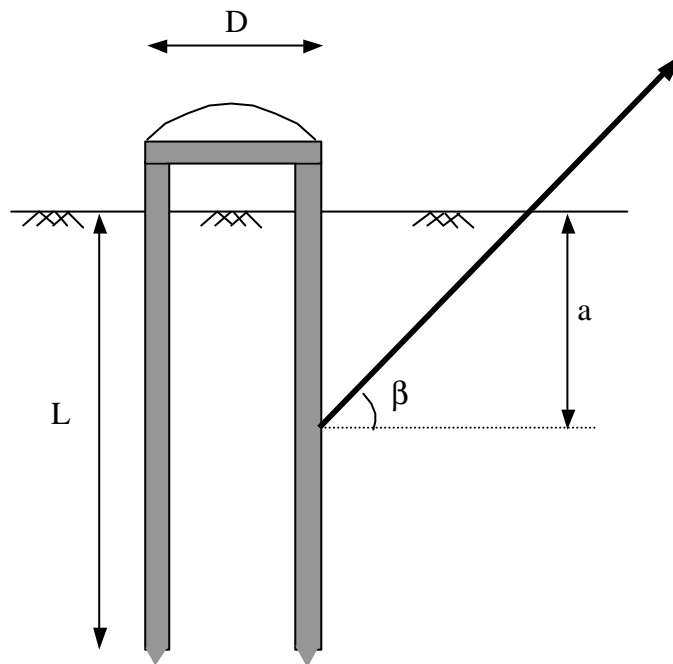
In association with



1. Introduction

Suction anchors (or suction piles) are deep water anchors for floating structures or offshore oil installations. The pile consists of a hollow cylinder which has a top cap and a relatively thin wall.

Installing the pile involves initial penetration into the sea-bed under self weight. The pressure in the water trapped inside the pile, between the mud-line and the top cap, is then lowered by pumping, to cause a positive differential water pressure across the top of the pile, thus forcing the pile further into the soil until its final position is reached.



2. Problem Specifications

Pile diameter, $D=6\text{m}$

Pile penetration, $L=13.5\text{m}$

Attachment point positions are:

$a=6.75\text{ m}$ (or $1/2$ depth L)

$a=9\text{m}$ (or $2/3$ of depth L)

$a=7.785\text{m}$ (just below mid point, considered to be optimum position)

Angle of inclination β is 0° (horizontal chain), 15° , 26° , 30° , 45° , 90° (vertical chain)

Load applied consists of 50 unequal load increments with maximum load= 10000kN

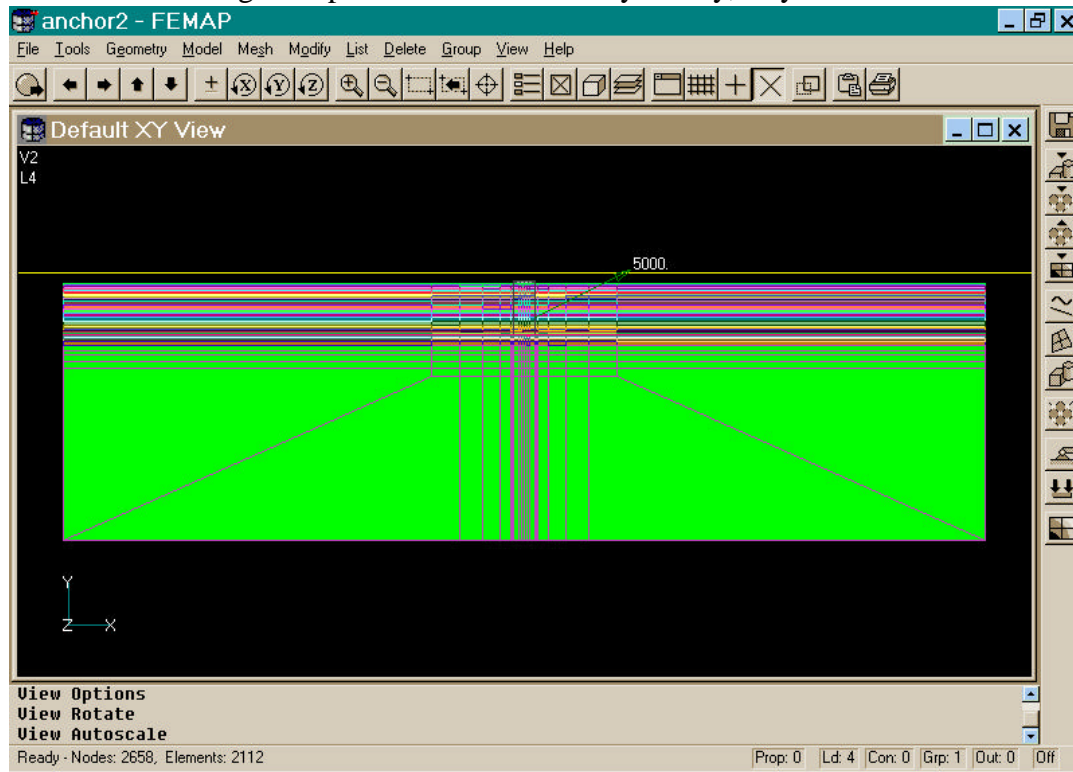
The undrained shear strength, C_u , at mud-line is 3Kpa and it is assumed to increase with depth by a rate of 1.85 .

Young's modulus at mud-line is assumed to be 300 KPa and it is assumed to increase with depth by a rate of 185 .

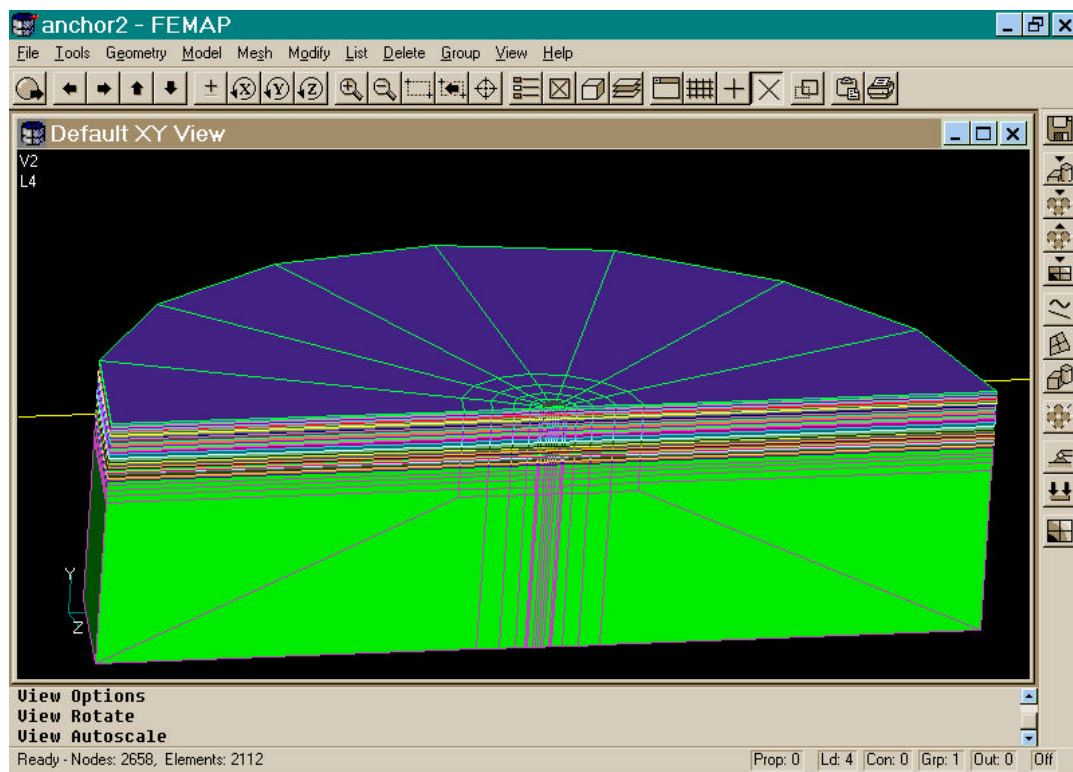
The pile shell's thickness is 3cm . The pile is also assumed to be very stiff, with $E=2.1\text{E}8$

3. Finite Element Mesh

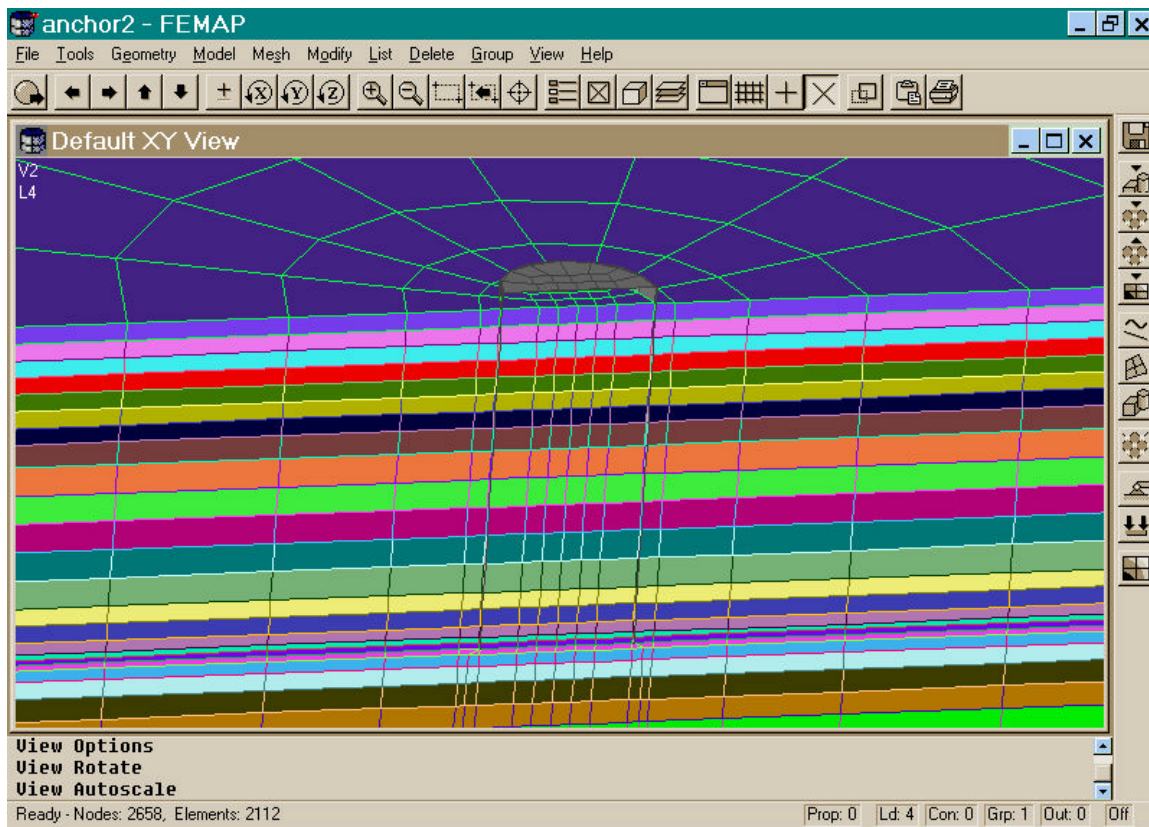
This was done using Femap Basic edition. Due to symmetry, only half the model was considered due



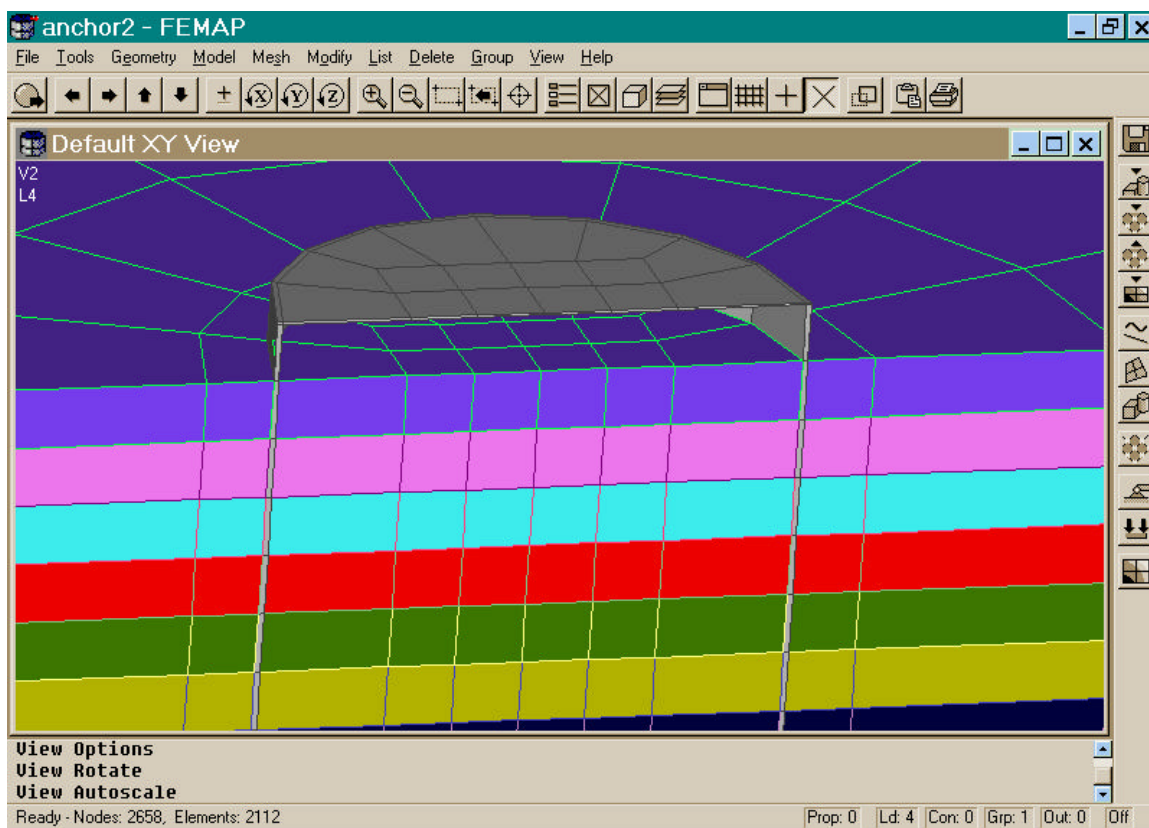
X-Y elevation showing full mesh



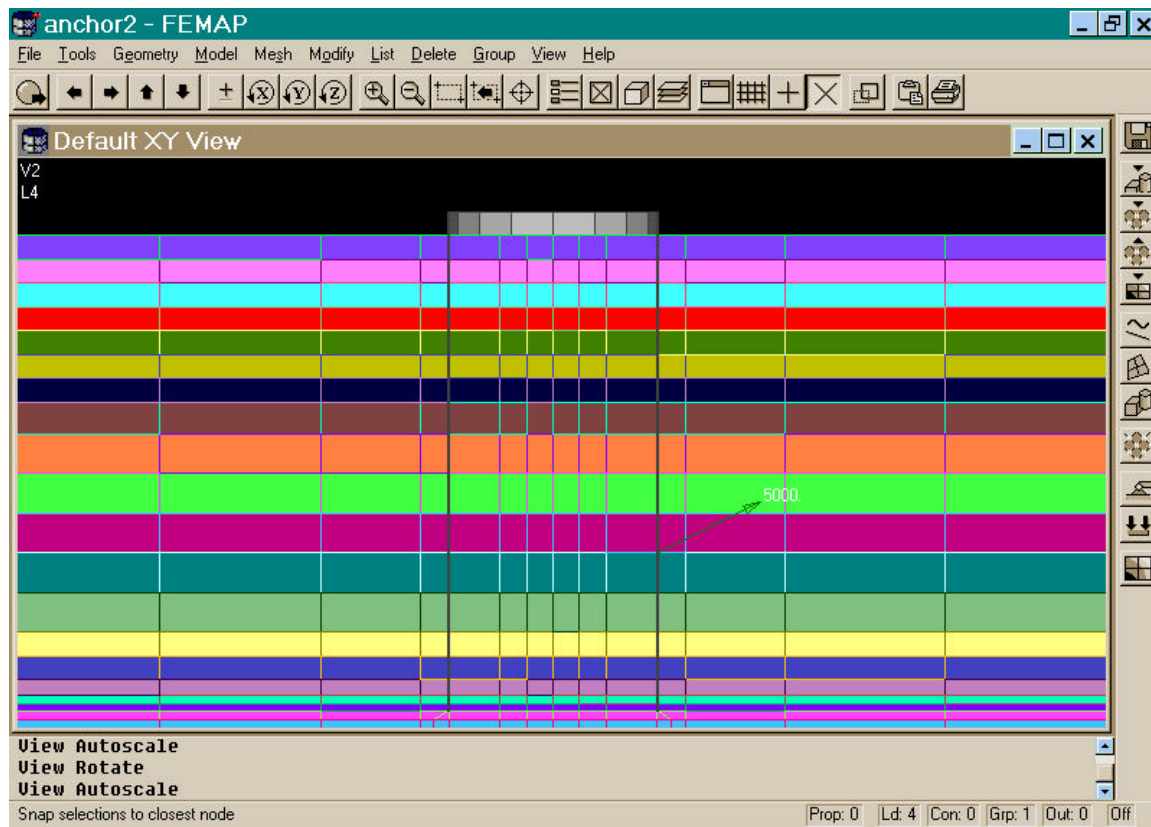
3D view of full mesh



View showing suction pile



View showing suction pile cap

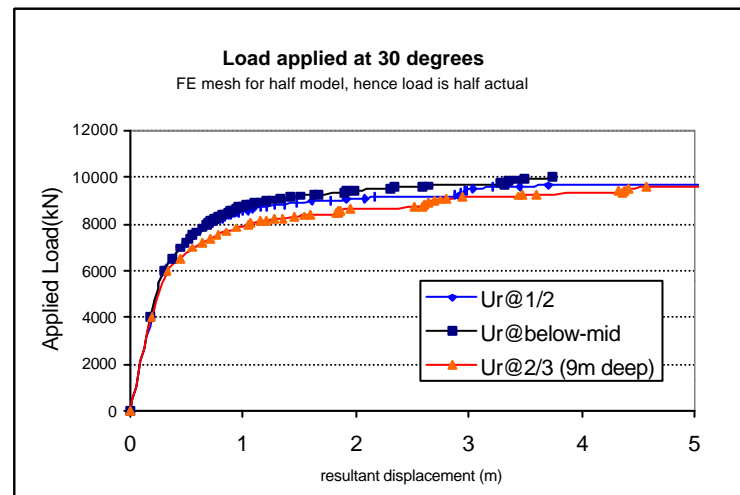
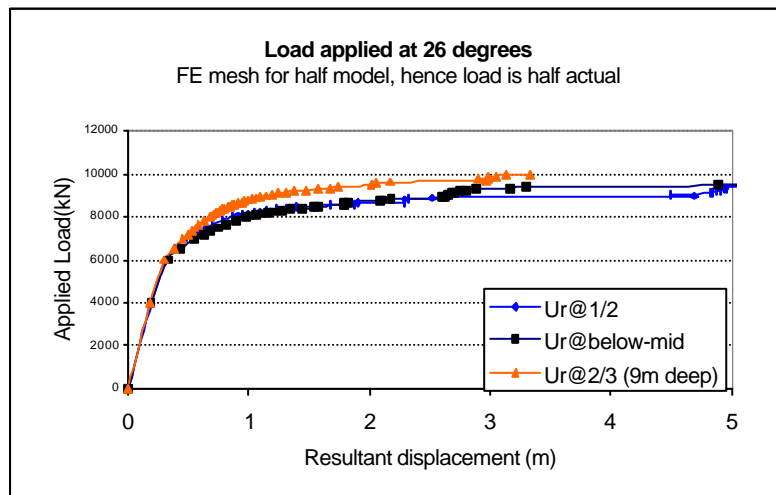
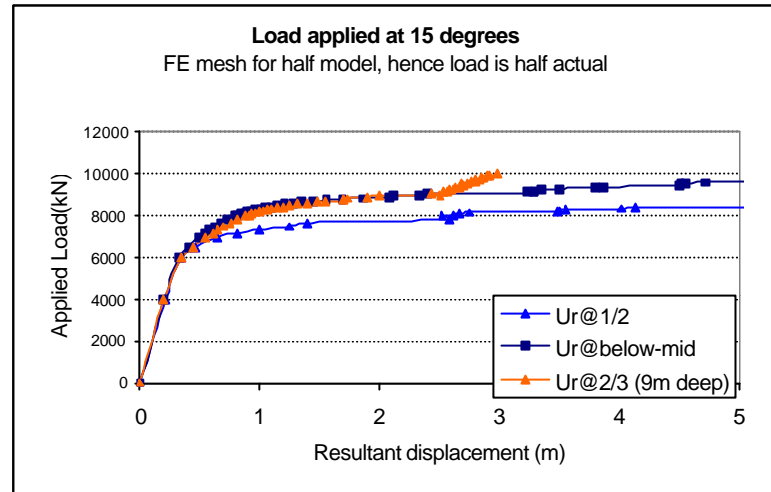
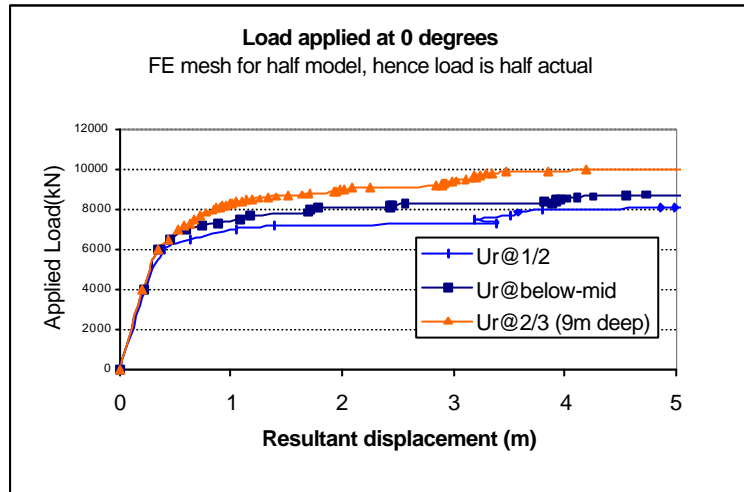


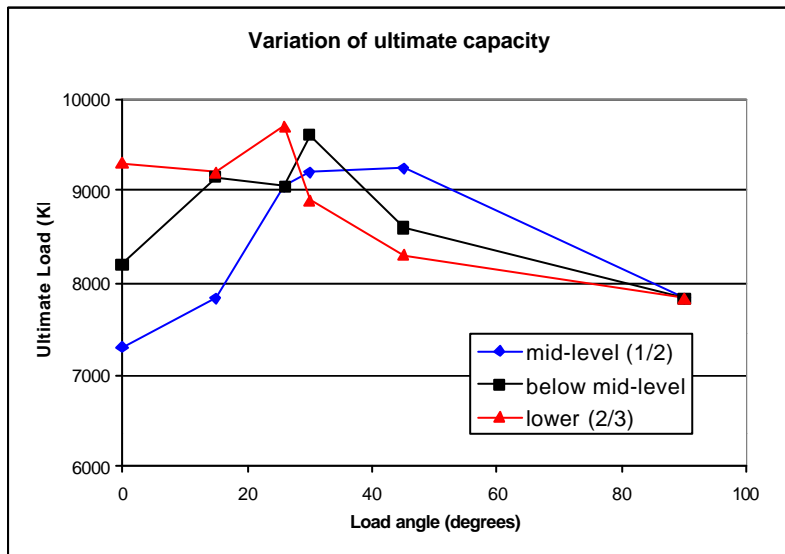
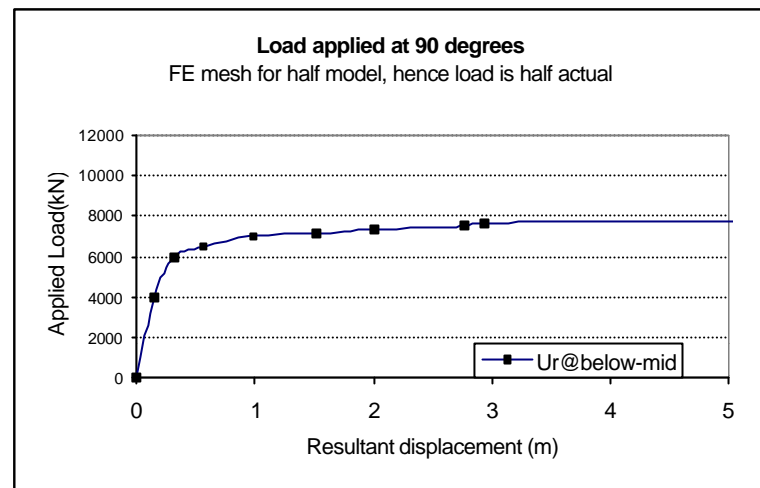
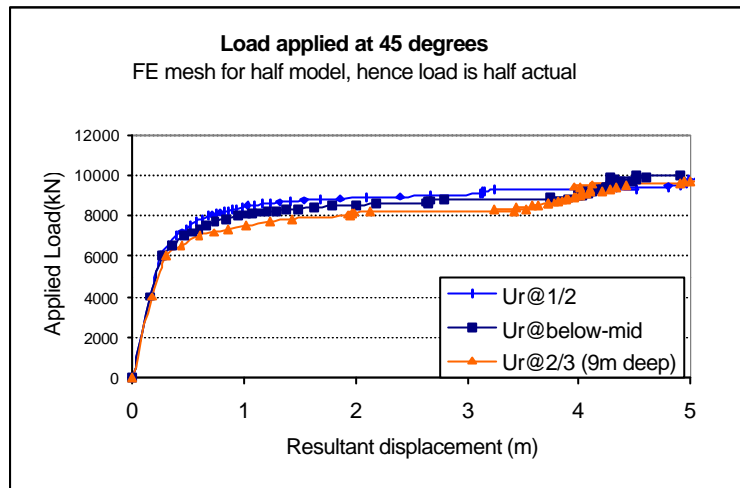
X-Y elevation view showing pile and loading point

The properties given in the Problem Specification section above are used. A von Mises undrained material is used for the soil, with Poisson's ratio=0.49.

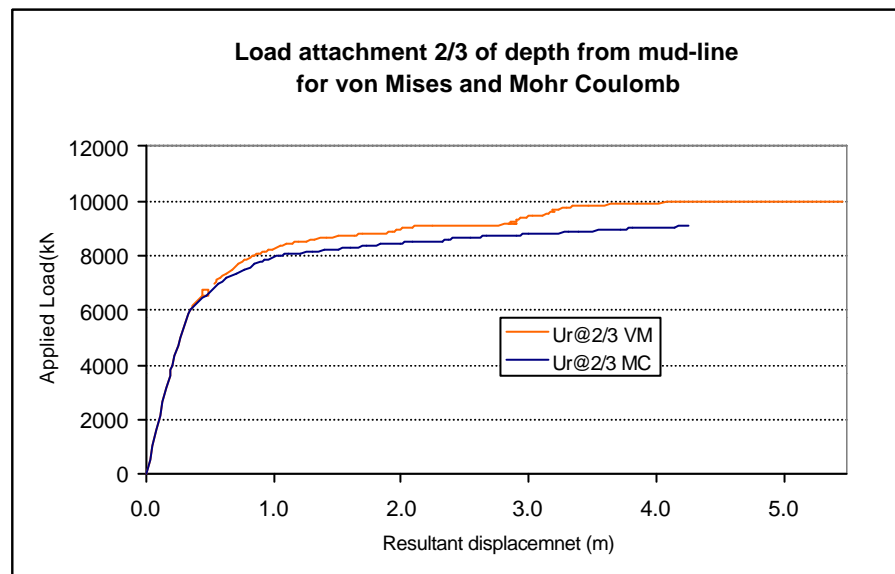
4. Finite Element Results

The following charts show FE results for cases with different load attachment point and angle. A von Mises material is used for all of these cases





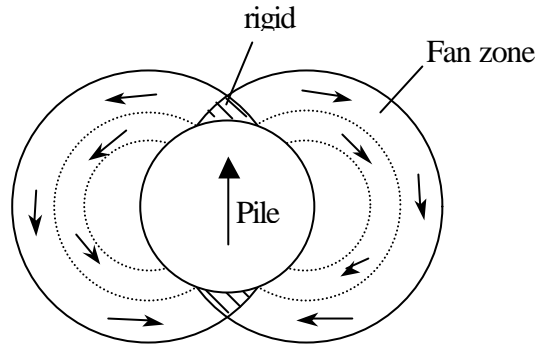
Comparison of ultimate anchor pull-out force for different anchoring points and angles.



Comparison between von Mises results and Mohr Coulomb results, for the case of horizontal pull at 2/3 of penetration depth

5. Analytical solution using upper bound theory

According to Randolph and Houlsby (1984)¹, the plastic flow around a pile loaded laterally, may be described as follows:



The equation for the limiting load for the above mechanism is given as:

$$P_u = c_u d [\mathbf{p} + 2\Delta + 4\cos\{(\mathbf{p} - \Delta)/4\} [\sqrt{2} + \sin\{(\mathbf{p} - \Delta)/4\}]] \quad (1)$$

where d is the pile diameter, and c_u is the undrained shear strength

The pile soil adhesion is defined by:

$$\sin \Delta = f_s / c_u \quad (2)$$

where f_s is the limiting pile friction which is less than or equal to the shear strength of the soil.

Assuming full adhesion, we get

$$\sin \Delta = 1 \quad \therefore \Delta = \frac{\mathbf{p}}{2} \quad (3)$$

Substituting to solve equation we get

$$P_u = c_u d \times 12.924 \text{ KN per meter depth}$$

The average C_u for this problem is 15.5 Kpa (linear variation of $C_u=3\text{Kpa}$ at the top of pile to 27.98 Kpa at the bottom), and as the diameter is 6m, we get,

$$P_u = 1202 \text{ KN per meter depth}$$

The depth of the pile is 13.5m, therefore the total force is

$$P_u(\text{total}) = 16225 \text{ KN}$$

We could also add the resistance at the base of the pile, which is simply the area times C_u , (or $\mathbf{p}^2 \times c_u$). We could use the maximum shear strength at the base, which is $C_u=27.98 \text{ Kpa}$. This gives a total force of

$$P_u(\text{total}) = 16225 + 791 = 17017 \text{ KN}$$

The FE solution for lateral loading (ie $\beta=0^\circ$), we have

$$P \text{ (for 1/2 depth)} = 14600 \text{ KN}$$

$$P \text{ (for below mid-depth)} = 16400 \text{ KN}$$

$$P \text{ (for 2/3 of depth)} = 18600 \text{ KN}$$

¹ Geotechnique 4 of 1984 "The limiting pressure on a circular pile loaded laterally"

6. Conclusions

- The FE solution for a middle attachment point loaded horizontally can be compared with the upper bound solution of laterally loaded pile. For this analysis the FE solution of $\sigma_{\theta} = 0$ at a point below mid-depth is about 4% lower than the upper bound solution.
- A more complex upper bound solution is necessary for cases in which the load is applied at an angle, due to the rotation of the pile.
- Pull out capacity tends to reduce when the angle of load attachment approaches a horizontal level. This indicates that the vertical resistance is the predominant component for such deep piles.
- All the analyses above were carried out using reduced integration (ie 2x2x2 Gauss points). Use of full integration produced a slightly higher collapse load.
- Use of Mohr Coulomb is preferred over use of von Mises material. The Mohr-Coulomb yield surface in the π -plane is slightly smaller giving a lower collapse load.

